

READY, SET, GO!

Name _____

Period _____

Date _____

READY

A golf-pro practices his swing by driving golf balls off the edge of a cliff into a lake. The height of the ball above the lake (measured in meters) as a function of time (measured in seconds and represented by the variable t) from the instant of impact with the golf club is

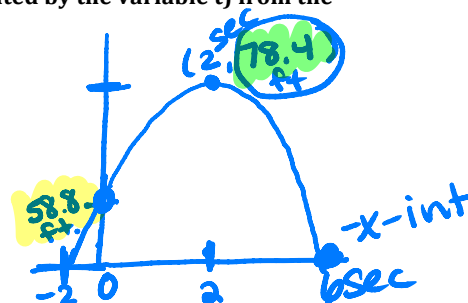
$$58.8 + 19.6t - 4.9t^2$$

The expressions below are equivalent:

$$-4.9t^2 + 19.6t - 58.8 \quad \text{standard form}$$

$$-4.9(t - 6)(t + 2) \quad \text{factored form}$$

$$-4.9(t - 2)^2 + 78.4 \quad \text{vertex form}$$



- Which expression is the most useful for finding how many seconds it takes for the ball to hit the water? Why?
Factored form gives the x-intercepts
- Which expression is the most useful for finding the maximum height of the ball? Justify your answer.
Vertex Form gives the maximum
- If you wanted to know the height of the ball at exactly 3.5 seconds, which expression would help the most to find the answer? Why?
Any form, plug in 3.5 for x and solve for y. (Factored form)
- If you wanted to know the height of the cliff above the lake, which expression would you use? Why?
Standard Form tells the y-intercept

SET

Topic: Finding multiple representations of a quadratic

One form of a quadratic function is given. Fill-in the missing forms.

| <p>5 a. Standard Form</p> $y = x^2 + 2x - 15$ | <p>b. Vertex Form</p> $y = (x + 1)^2 - 16$ | <p>c. Factored Form</p> $y = (x + 5)(x - 3)$ | | | | | | | | | | | |
|---|--|--|----|---|----|-----|----|-----|---|-----|---|---|-----------------|
| <p>d. Table (Include the vertex and at least 2 points on each side of the vertex.)</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr><td>-5</td><td>0</td></tr> <tr><td>-2</td><td>-15</td></tr> <tr><td>-1</td><td>-16</td></tr> <tr><td>0</td><td>-15</td></tr> <tr><td>3</td><td>0</td></tr> </tbody> </table> <p>Show the first differences and the second differences.</p> | x | y | -5 | 0 | -2 | -15 | -1 | -16 | 0 | -15 | 3 | 0 | <p>e. Graph</p> |
| x | y | | | | | | | | | | | | |
| -5 | 0 | | | | | | | | | | | | |
| -2 | -15 | | | | | | | | | | | | |
| -1 | -16 | | | | | | | | | | | | |
| 0 | -15 | | | | | | | | | | | | |
| 3 | 0 | | | | | | | | | | | | |

$$y = (x^2 + 2x + 1) - 15 - 1$$

$$(x + 1)^2 - 16$$

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$$y = -3(x^2 - 2x + 1) + 3$$

$$y = -3x^2 + 6x - 3 + 3$$

Lesson 9

| <p>6 a. <i>Standard Form</i> $y = -3x^2 + 6x$</p> | <p>b. <i>Vertex Form</i> $y = -3(x - 1)^2 + 3$</p> | <p>c. <i>Factored Form</i> $y = -3x(x - 2)$</p> | | | | | | | |
|--|---|--|---|---|---|---|---|---|------------------------|
| <p>d. <i>Table</i> (Include the vertex and at least 2 points on each side of the vertex.)</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">x</th> <th style="border-bottom: 1px solid black; padding: 5px;">y</th> </tr> </thead> <tbody> <tr> <td style="border-right: 1px solid black; text-align: center; padding: 5px;">0</td> <td style="text-align: center; padding: 5px;">0</td> </tr> <tr> <td style="border-right: 1px solid black; text-align: center; padding: 5px;">1</td> <td style="text-align: center; padding: 5px;">3</td> </tr> <tr> <td style="border-right: 1px solid black; text-align: center; padding: 5px;">2</td> <td style="text-align: center; padding: 5px;">0</td> </tr> </tbody> </table> <p>Show the first differences and the second differences.</p> | x | y | 0 | 0 | 1 | 3 | 2 | 0 | <p>e. <i>Graph</i></p> |
| x | y | | | | | | | | |
| 0 | 0 | | | | | | | | |
| 1 | 3 | | | | | | | | |
| 2 | 0 | | | | | | | | |

| <p>7 a. <i>Standard Form</i> $y = -x^2 + 10x - 25$</p> | <p>b. <i>Vertex Form</i> $y = -(x - 5)^2$</p> | <p>c. <i>Factored Form</i> $y = -(x - 5)(x - 5)$</p> | | | |
|--|--|---|---|---|------------------------|
| <p>d. <i>Table</i> (Include the vertex and at least 2 points on each side of the vertex.)</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">x</th> <th style="border-bottom: 1px solid black; padding: 5px;">y</th> </tr> </thead> <tbody> <tr> <td style="border-right: 1px solid black; text-align: center; padding: 5px;">5</td> <td style="text-align: center; padding: 5px;">0</td> </tr> </tbody> </table> <p>Show the first differences and the second differences.</p> | x | y | 5 | 0 | <p>e. <i>Graph</i></p> |
| x | y | | | | |
| 5 | 0 | | | | |

| <p>8 a. <i>Standard Form</i> $y = x^2 + 5x + 6$</p> | <p>b. <i>Vertex Form</i> $y = (x + \frac{5}{2})^2 - \frac{1}{4}$</p> | <p>c. <i>Factored Form</i> $y = (x + 2)(x + 3)$</p> | | | |
|---|---|--|--|--|------------------------|
| <p>d. <i>Table</i> (Include the vertex and at least 2 points on each side of the vertex.)</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="border-right: 1px solid black; border-bottom: 1px solid black; padding: 5px;">x</th> <th style="border-bottom: 1px solid black; padding: 5px;">y</th> </tr> </thead> <tbody> <tr> <td style="border-right: 1px solid black; height: 100px;"></td> <td></td> </tr> </tbody> </table> <p>Show the first differences and the second differences.</p> | x | y | | | <p>e. <i>Graph</i></p> |
| x | y | | | | |
| | | | | | |

$$y = (x^2 + 5x + \frac{25}{4}) + 6 - \frac{25}{4}$$

$$y = (x + \frac{5}{2})^2 - \frac{1}{4}$$

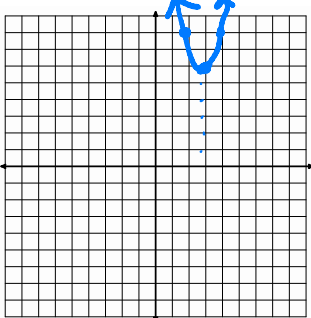
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$$y = 2(x-3)^2 - 6$$

$$y = 2(x^2 - 6x + 9) - 6$$

$$y = 2x^2 - 12x + 18 - 6$$

$$y = 2x^2 - 12x + 12$$

| <p>9 a. <i>Standard Form</i> $y = 2x^2 - 12x + 12$</p> | <p>b. <i>Vertex Form</i> $y = 2(x-3)^2 - 6$</p> | <p>c. <i>Factored Form</i> Skip this for now</p> | | | | | | | | | | | | | | | | |
|--|--|--|---|---|----|---|---|---|----|---|----|---|----|---|---|---|----|---|
| <p>d. <i>Table</i></p> <table border="1" style="display: inline-table; margin-right: 20px;"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr><td>0</td><td>12</td></tr> <tr><td>1</td><td>2</td></tr> <tr><td>2</td><td>-4</td></tr> <tr><td>3</td><td>-6</td></tr> <tr><td>4</td><td>-4</td></tr> <tr><td>5</td><td>2</td></tr> <tr><td>6</td><td>12</td></tr> </tbody> </table> <p style="margin-left: 100px;">$y = 2(x-3)^2 - 6$</p> <p style="margin-left: 100px;">+2 +6 +8</p> <p>Show the first differences and the second differences.</p> | | x | y | 0 | 12 | 1 | 2 | 2 | -4 | 3 | -6 | 4 | -4 | 5 | 2 | 6 | 12 | <p>e. <i>Graph</i></p>  |
| x | y | | | | | | | | | | | | | | | | | |
| 0 | 12 | | | | | | | | | | | | | | | | | |
| 1 | 2 | | | | | | | | | | | | | | | | | |
| 2 | -4 | | | | | | | | | | | | | | | | | |
| 3 | -6 | | | | | | | | | | | | | | | | | |
| 4 | -4 | | | | | | | | | | | | | | | | | |
| 5 | 2 | | | | | | | | | | | | | | | | | |
| 6 | 12 | | | | | | | | | | | | | | | | | |

GO

Topic: Factoring Quadratics

Verify each factorization by multiplying.

10. $x^2 + 12x - 64 = (x + 16)(x - 4)$
 $x^2 - 4x + 16x - 64$
 $x^2 + 12x - 64$

11. $x^2 - 64 = (x + 8)(x - 8)$
 $= x^2 - 8x + 8x - 64$
 $= x^2 - 64$

12. $x^2 + 20x + 64 = (x + 16)(x + 4)$
 $x^2 + 4x + 16x + 64$
 $x^2 + 20x + 64$

13. $x^2 - 16x + 64 = (x - 8)(x - 8)$
 $= x^2 - 8x - 8x + 64$
 $= x^2 - 16x + 64$

Factor the following quadratic expressions, if possible. (Some will not factor.)

14. $x^2 - 5x + 6$
 $(x-3)(x-2)$

15. $x^2 - 7x + 6$
 $(x-6)(x-1)$

16. $x^2 - 5x - 36$
 $(x-9)(x+4)$

17. $m^2 + 16m + 63$
 $(m+7)(m+9)$

18. $s^2 - 3s - 1$
 prime

19. $x^2 + 7x + 2$
 prime

20. $x^2 + 14x + 49$
 $(x+7)^2$

21. $x^2 - 9$
 $(x+3)(x-3)$

22. $c^2 + 11c + 3$
 prime

23. Which quadratic expression above could represent the area of a square? Explain.

#20 factors are the same

24. Would any of the expressions above NOT be the side-lengths for a rectangle? Explain.

#18, #19, #22

They do not factor.

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