

Simplifying Trigonometric Expressions

Simplify each of the following.

1. $\sec x \cos x$

2.
$$\frac{\sin(-x)}{\cos(-x)}$$

3. $\tan^2 x - \sec^2 x$

4.
$$\frac{1 - \cos^2 x}{\sin x}$$

5. $\cot x \sin x$

6.
$$\frac{\sin\left(\frac{\pi}{2} - x\right)}{\cos\left(\frac{\pi}{2} - x\right)}$$

7. $\sin x \sec x$

8. $\cos^2 x (\sec^2 x - 1)$

9.
$$\frac{\sec^2 x - 1}{\sin^2 x}$$

10. $\cot x \sec x$

11. $\sec^4 x - \tan^4 x$

12.
$$\frac{\cos^2\left(\frac{\pi}{2} - x\right)}{\cos x}$$

13. $\tan \theta \csc \theta$

14. $\sin \theta (\csc \theta - \sin \theta)$

15. $\cos \beta \tan \beta$

16. $\sec \alpha \frac{\sin \alpha}{\tan \alpha}$

17.
$$\frac{\cot x}{\csc x}$$

18.
$$\frac{\csc \theta}{\sec \theta}$$

19. $\sec^2 x (1 - \sin^2 x)$

20.
$$\frac{1}{\tan^2 x + 1}$$

$$21. \frac{\sin(-x)}{\cos x}$$

$$22. \frac{\tan^2 x}{\sec^2 x}$$

$$23. \cos\left(\frac{\pi}{2} - x\right) \sec x$$

$$24. \cot\left(\frac{\pi}{2} - x\right) \cos x$$

$$25. \frac{\cos^2 y}{1 - \sin y}$$

$$26. \cos t(1 + \tan^2 t)$$

$$27. \tan^2 x - \tan^2 x \sin^2 x$$

$$28. \sec^2 x \tan^2 x + \sec^2 x$$

$$29. \sec^2 x \sin^2 x - \sin^2 x$$

$$30. \frac{\sec^2 x - 1}{\sec x - 1}$$

$$31. \tan^4 x + 2 \tan^2 x + 1$$

$$32. 1 - 2 \cos^2 x + \cos^4 x$$

$$33. \sin^4 x - \cos^4 x$$

$$34. \csc^3 x - \csc^2 x - \csc x + 1$$

Perform the indicated operation and simplify.

$$35. (\sin x + \cos x)^2$$

$$36. (\cot x + \csc x)(\cot x - \csc x)$$

$$37. (\sec x - 1)(\sec x + 1)$$

$$38. (3 - 3 \sin x)(3 + 3 \sin x)$$

$$39. \frac{1}{1 + \cos x} + \frac{1}{1 - \cos x}$$

$$40. \frac{1}{\sec x + 1} - \frac{1}{\sec x - 1}$$

$$41. \frac{\cos x}{1 + \sin x} + \frac{1 + \sin x}{\cos x}$$

$$42. \tan x - \frac{\sec^2 x}{\tan x}$$