

Sum and Difference Formulas

$$\sin(u \pm v) = \sin u \cos v \pm \cos u \sin v$$

$$\cos(u \pm v) = \cos u \cos v \mp \sin u \sin v$$

$$\tan(u \pm v) = \frac{\tan u \pm \tan v}{1 \mp \tan u \tan v}$$

Use the sum or difference identity to find the exact value.

1. $\sin 15^\circ$

2. $\tan 15^\circ$

3. $\sin 75^\circ$

4. $\cos 75^\circ$

5. $\cos \frac{\pi}{12}$

6. $\sin \frac{7\pi}{12}$

7. $\tan \frac{5\pi}{12}$

8. $\tan \frac{11\pi}{12}$

9. $\cos \frac{7\pi}{12}$

10. $\sin \frac{-\pi}{12}$

Write the expression as the sine, cosine, or tangent of an angle

$$11. \quad \sin 42^\circ \cos 17^\circ - \cos 42^\circ \sin 17^\circ$$

$$12. \quad \cos 94^\circ \cos 18^\circ + \sin 94^\circ \sin 18^\circ$$

$$13. \quad \sin \frac{\pi}{5} \cos \frac{\pi}{2} + \sin \frac{\pi}{2} \cos \frac{\pi}{5}$$

$$14. \quad \sin \frac{\pi}{3} \cos \frac{\pi}{7} - \cos \frac{\pi}{3} \sin \frac{\pi}{7}$$

$$15. \quad \frac{\tan 19^\circ + \tan 47^\circ}{1 - \tan 19^\circ \tan 47^\circ}$$

$$16. \quad \frac{\tan \frac{\pi}{5} - \tan \frac{\pi}{3}}{1 + \tan \frac{\pi}{5} \tan \frac{\pi}{3}}$$

$$17. \quad \cos x \cos \frac{\pi}{7} + \sin x \sin \frac{\pi}{7}$$

$$18. \quad \cos x \cos \frac{\pi}{7} - \sin x \sin \frac{\pi}{7}$$

$$19. \quad \sin 3x \cos x - \cos 3x \sin x$$

$$20. \quad \cos 7y \cos 3y - \sin 7y \sin 3y$$

$$21. \quad \frac{\tan 2y + \tan 3x}{1 - \tan 2y \bullet \tan 3x}$$

$$22. \quad \frac{\tan 3\alpha - \tan 2\beta}{1 + \tan 3\alpha \bullet \tan 2\beta}$$