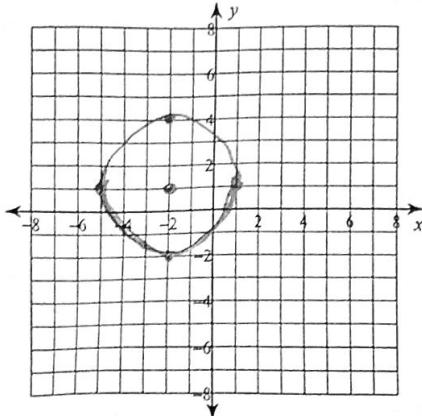


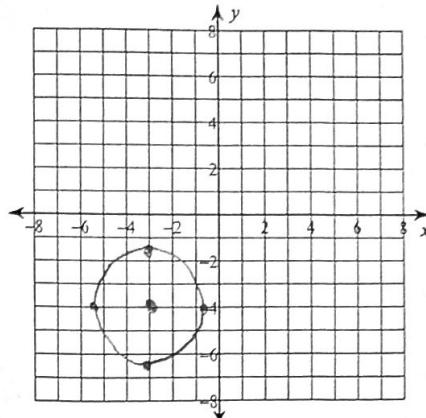
## Circles

Identify the center and radius of each. Then sketch the graph.

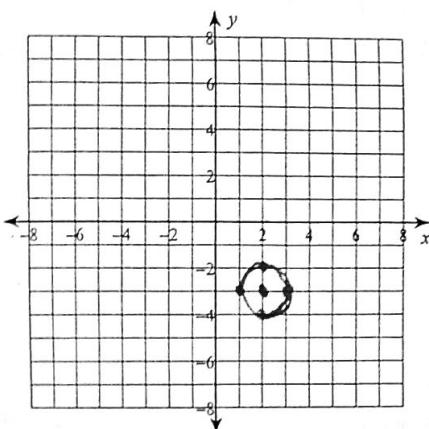
1)  $(x + 2)^2 + (y - 1)^2 = 9$

center  $(-2, 1)$   
 $r = 3$ 

2)  $(x + 3)^2 + (y + 4)^2 = 5$

center  $(-3, -4)$   
 $r = \sqrt{5}$ 

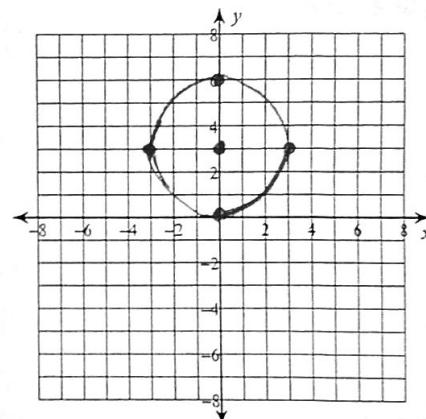
3)  $(x - 2)^2 + (y + 3)^2 = 1$

center  $(2, -3)$   
 $r = 1$ 

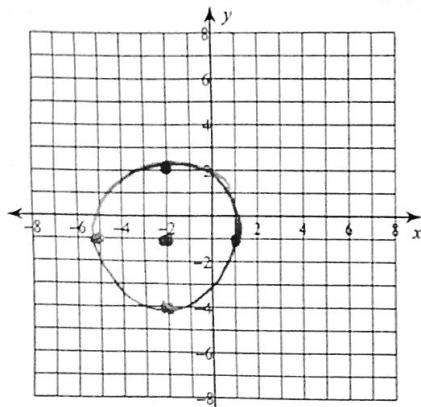
4)  $x^2 + y^2 - 6y = 0$

$x^2 + y^2 - 6y + 9 = +9$

$x^2 + (y - 3)^2 = 9$

center  $(0, 3)$   
 $r = 3$ 

5)  $x^2 + y^2 + 4x + 2y - 4 = 0$



$x^2 + 4x + 4 + y^2 + 2y + 1 = 4 + 4 + 1$

$(x + 2)^2 + (y + 1)^2 = 9$

center  $(-2, -1)$ 

$r = 3$

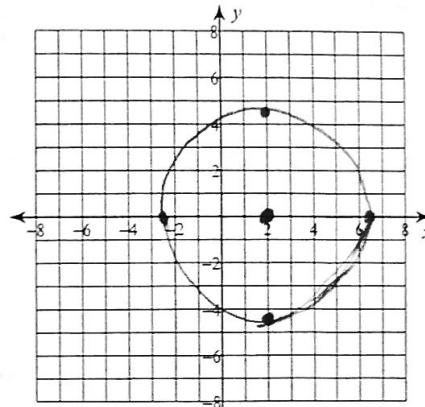
6)  $x^2 + y^2 - 4x - 14 = 0$

$x^2 - 4x + 4 + y^2 = 14 + 4$

$(x - 2)^2 + y^2 = 18$

center  $(2, 0)$ 

$r = 3\sqrt{2}$



Use the information provided to write the standard form equation of each circle.

- 7) Center:  $(-13, -14)$   
Radius: 1

$$(x+13)^2 + (y+14)^2 = 1$$

- 8) Center:  $(15, -8)$   
Area:  $16\pi$

$$(x-15)^2 + (y+8)^2 = 16$$

$$A = \pi r^2$$

$$\pi r^2 = 16\pi$$

$$r = 4$$

- 9) Center:  $(-2, 9)$   
Point on Circle:  $(-5, 18)$

$$(x+2)^2 + (y-9)^2 = r^2$$

$$(-5+2)^2 + (18-9)^2 = r^2$$

$$(-3)^2 + 9^2 = r^2$$

$$9 + 81 = r^2$$

$$90 = r^2$$

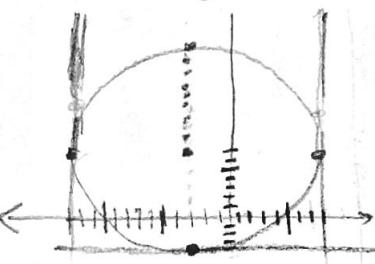
$$(x+2)^2 + (y-9)^2 = 90$$

- 11) Center lies in the second quadrant

Tangent to  $x = -14$ ,  $y = -4$ , and  $x = 8$

center  $(-3, -4)$   
 $r = 11$

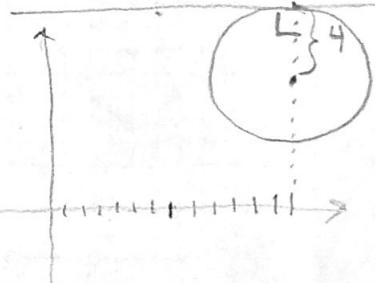
$$(x+3)^2 + (y+4)^2 = 121$$



- 10) Center:  $(13, 7)$   
Tangent to  $y = 11$

$$(x-13)^2 + (y-7)^2 = 4^2$$

$$(x-13)^2 + (y-7)^2 = 16$$



- 12) Ends of a diameter:  $(11, -6)$  and  $(1, 14)$

$$d = \sqrt{(11-1)^2 + (-6-14)^2}$$

$$d = \sqrt{100 + 400} = \sqrt{500} = 10\sqrt{5}$$

$$r = 5\sqrt{5}$$

$$\text{center } \left(\frac{11+1}{2}, \frac{-6+14}{2}\right)$$

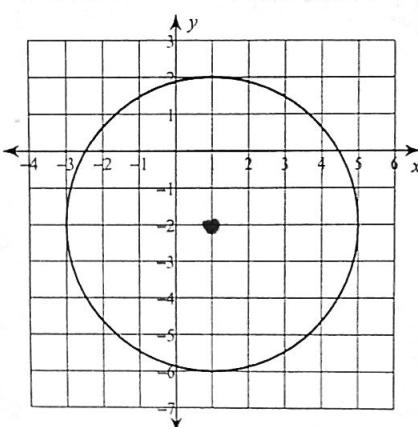
$$(6, 4)$$

$$(x-6)^2 + (y-4)^2 = (5\sqrt{5})^2$$

$$(x-6)^2 + (y-4)^2 = 125$$

Use the information provided to write the general conic form equation of each circle.

13)



Standard form  
 $(x-1)^2 + (y+2)^2 = 16$

general conic form  
 $x^2 - 2x + 1 + y^2 + 4y + 4 = 16$

$x^2 + y^2 - 2x + 4y - 11 = 0$

- 14) Three points on the circle:  
 $(7, -4)$ ,  $(-3, -4)$ , and  $(6, -7)$

center  $(2, -4)$

Standard form  
 $(x-2)^2 + (y+4)^2 = 25$

$r = 5$

$$x^2 - 4x + 4 + y^2 + 8y + 16 = 25$$

$$x^2 + y^2 - 4x + 8y - 5 = 0$$

general conic form