

Notes 9.4 – Geometric Series**Sum of a Finite Geometric Series:**

$$S_n = a_1 \frac{1 - r^n}{1 - r}$$

Sum of an Infinite Geometric Series:

$$\sum_{k=1}^{\infty} a_1 \cdot r^{n-1} = \frac{a_1}{1 - r}, \text{ if \& only if } |r| < 1$$

If an infinite series has a sum it is _____

If it does not it is called _____

Ex1) Find the sum of the given geometric series

a) $\sum_{n=1}^{11} 4 \left(-\frac{1}{3}\right)^{n-1}$

b) $5 + 15 + 45 + \dots + 98415$

c) $1 + 3 + 9 + \dots + 2187$

d) $1 - \frac{1}{2} + \frac{1}{4} - \frac{1}{8} + \dots - \frac{1}{512}$

Ex2) Determine if the following series converge. If they do converge find the sum:

a) $\sum_{n=1}^{\infty} 3(0.75)^{n-1}$

b) $\sum_{n=0}^{\infty} \left(-\frac{4}{5}\right)^{n-1}$

c) $\sum_{n=1}^{\infty} \left(\frac{\pi}{2}\right)^n$

d) $\sum_{n=1}^{\infty} \left(\frac{1}{2}\right)^{n-1}$